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# Efficient ~~and~~ Privacy-preserving Location Based Service Provisioning in Internet of Things

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**Abstract:** Location-based Services (LBS) have become very popular with the rapid development of Internet of Things (IoT) technology and the ubiquitous use of smartphones and social networks in our daily lives. Although users can enjoy a lot of flexibility and conveniences from the LBS in IoT, they may also lose their privacy. Untrusted or malicious LBS servers having all users' information and thus can track users in various ways or release personal data to third parties. In this work, we first analyze the dummy-location selection (DLS) algorithm—an efficient location privacy preservation approach and design an attack algorithm for DLS (ADLS), an emerging IoT for testing security. For efficiently preserving user's location privacy, we propose a novel dummy location privacy-preserving (DLP) algorithm, which considers both of the computational costs and various privacy requirements of different users. We conduct extensive simulation experiments to evaluate the efficiency of the proposed schemes. Evaluation results show that the ADLS algorithm has a high probability of identifying the user's real location out from chosen dummy locations in the DLS algorithm. When compared with the DLS algorithm, the results show that our proposed DLP algorithm not only has a lower probability of revealing the user's real location, but also can reduce the computational cost and efficiency (i.e., time, speed, accuracy, and—complexity) while providing the same privacy level as DLS algorithm.

**Key words:** Privacy preserving; Location privacy; Location based services;  $k$ -anonymization

## 1. INTRODUCTION

In recent years, there has been a rapid development in mobile technology resulting in the immense popularity of a variety of mobile devices and social networks and contributions to the development of emerging IoT services [1-4]. Many of these developments rely on the utilization of location-based services (LBS) or LBS applications. Today's smartphones have built in Global Positioning System (GPS) modules that have powerful computation ability to process users' location information. Users can download many of LBS applications from various sites such as the Apple Store or Google Play Store. With the help of these applications, users can send their queries which include their identities, locations (e.g., got by the GPS module using localization techniques), interests, and

other information (e.g., time, query range) to LBS server, for getting the required information such as the nearest shopping mall, supermarket, restaurant. However, while enjoying the convenience or entertainment from the LBS server, users are susceptible to the leakage of their sensitive information in IoT leading to the risks of loss of privacy. Based on a user's LBS queries, an adversary not only can link their identity with locations and interests, but also infer more private information about the user. For example, if a user often reveals his/her location close to a hospital when requesting LBS in IoT, the location information could be used by an adversary to conjecture that the user may have some health problems. Since the untrusted LBS server has all the information about users such as where they are at what time, what kind of queries they submit, etc., the LBS server may use the information to track users in all kinds of ways or reveal users' personal data to third parties. Therefore, it's necessary to pay more attention to users' location privacy, particularly for a data-driven IoT service that delivers the requirements for IoT and big data fusion.

As large amount of data from different sources are gathered and processed, the IoT may have significant impact on users' privacy. Moreover, considering the increasing trend to collect more individual and personalized data in IoT, there are many problems regarding the impact on individuals' privacy from a legal perspective [42]. The data handling or processing of Internet of Things (IoT) is greatly impacted by location information and in turn greatly impact location privacy. Since location information is a major component in effective inventory and supply chains, efficient transportation systems, context-aware mobile applications, and numerous other IoT systems [43]. Furthermore, privacy attacks and harmful consequences can occur when sensitive location information is concealed or controlled without users' consent, which pose challenges for IoT security and privacy [44-46].

A large number of approaches [5-17] have been proposed to address the privacy preservation issue in location based services. Many of them are based on the cloaking technique, which employs the  $k$ -anonymity model to protect user's location privacy. The  $k$ -anonymity model is an important technique to protect user's location privacy in LBS, it can ensure that a user is identified with a probability of (only)  $1/k$ . To achieve  $k$ -anonymity in LBS, a user first submits a query

to a centralized location anonymizer. Then, the location anonymizer enlarges the queried location into a bigger Cloaking Region (CR) for covering many other users (at least  $k-1$ ) geographically distributed. Finally, the location anonymizer sends the query to the LBS server. However, since this technique relies heavily on the location anonymizer, there will be a single point of failure. Moreover, since all users' queries must be processed by the location anonymizer, the location anonymizer may be a performance bottleneck.

To address this problem, the "dummy location" has been proposed and used to protect user's location privacy, which does not need any third party service. Dummy location is part of our emerging IoT service. Existing approaches [18-20] try to effectively generate dummy locations which cannot be distinguished by the LBS server. However, these approaches do not consider the side information [21], i.e., users' query probability related to location and time, or information related to the semantics of the query such as the gender and social status of the user. If the side information is obtained by an adversary, incredible chosen dummy locations such as lakes, swamps etc. may be easily filtered out by the adversary. Therefore, these algorithms for dummy locations generation cannot effectively achieve  $k$ -anonymity. The authors in [22] proposed a dummy location selection (DLS) algorithm for location privacy preservation, which considers the side information that may be exploited by attackers. However, the computational cost (i.e., time complexity) of the DLS algorithm is very high. As a result, how to select dummy locations is still a challenge, particularly for a data-driven IoT service whereby more complexity can be involved with volume, velocity, variety, veracity and validity. Locations based service is one of the major application for a data-driven IoT service and it contains highly sensitive data which needs to be protected. LBS based cloud applications needs to collect, process, and analyze geo-position data or send the required geo-locations instantly for millions of users in real-time. LBS is useful for many cases include identifying location in an unfamiliar territory and finding local important places for socialization. However, LBS based applications also come with risk of revealing personal information and data that may be tracked. Despite personal identification information may be hidden in the LBS services, the geo-localised history of user requests can act as a quasi-identifier which then can be used to identify personal information about individuals data and their locations. Hence, we need efficient strategies to hide this quasi-identification which can only be handled by dummy LBS data.

In this paper, we first analyze the performance of the well known DLS algorithm, which is an efficient location privacy preservation approach for a data-driven IoT service of users' queries in LBS. Then, we design an attack algorithm for DLS (ADLS), whose goal is to identify the user's real location out from the data-driven IoT service of chosen dummy locations in LBS. We also design a dummy location based privacy-preserving (DLP) algorithm for location privacy preservation

in LBS. Different from existing approaches, the DLP algorithm makes a tradeoff between computational cost (i.e., time complexity) and the privacy requirements of users. The main contributions of this research are as follows:

- We analyze the performance of the DLS algorithm, and design an attack algorithm for DLS (ADLS), whose goal is to identify the user's real location out from the data-driven IoT service of chosen dummy locations.
- We propose an entropy-based DLP algorithm, which selects dummy locations in a greedy manner making a tradeoff between computational cost (i.e., time complexity) and the privacy requirements for the data-driven IoT service in LBS.
- We analyze the performance on privacy preservation of our proposed DLP algorithm against the *colluding attack* and *inference attack*. These attacks are aimed to test robustness of our data-driven IoT service.
- We show our proof-of-concepts by using simulations. Simulation results demonstrate that the ADLS algorithm has a high probability of query recognition for the DLS algorithm. When compared with the DLS algorithm, the results show that the DLP algorithm can efficiently reduce the computational cost (i.e., time complexity) while providing the same privacy level as the DLS algorithm. Moreover, the DLP algorithm has a lower probability of query recognition (i.e., lower probability of losing users' privacy) compared to the DLS algorithm.

The remainder of this paper is organized as follows. Section 2 reviews the related work. Section 3 introduces the preliminaries and the system model. Section 4 gives the detailed analysis on the DLS algorithm. Section 5 presents the ADLS algorithm for identifying the user real location and evaluate its performance. Section 6 presents the detailed descriptions on our DLP algorithm and simulation results. Section 7 gives the discussions and explains how our contributions are relevant to the data-driven IoT service. Section 8 concludes this paper.

## 2. RELATED WORK

In this section, we describe recent researches related to privacy protection methods in location based services of IoT.

### 2.1 Privacy-preserving for IoT

Several recent researches have been conducted for the privacy-preserving for the IoT based services [47-55]. In order to handle the massive amount of data, the most convincing solution is the federation of the IoT and cloud computing. Henze, et al. presented an user-driven privacy enforcement approach for cloud-based services in the IoT, which focuses on privacy preserving for individual end-users [47]. The authors in [48] proposed PAgIoT, a Privacy-preserving Aggregation protocol suitable for IoT settings and enables multi-attribute aggregation for groups of entities while allowing for privacy-preserving value correlation. A lightweight privacy-preserving trust model had been

designed for minimizing privacy loss in the presence of untrusted service providers, so that providers can be prevented from disclosing information to third parties for secondary uses [49]. A conditional privacy-preserving authentication with access linkability (CPAL) for roaming service, to provide universal secure roaming service and multilevel privacy preservation [50]. The authors in [51] estimated the cost of breaking public key crypto systems when the adversary is limited by the available resources and time and presented the trade-off between the processing load for an IoT node versus the desired time span of privacy protection. Jin, et al., presented a framework for the realization of smart cities through the Internet of Things (IoT), which encompasses the complete urban information system and forms a transformational part of the existing cyber-physical system [52]. The authors in [53] proposed a privacy-by-design (PbD) framework that can guide software engineers to systematically assess the privacy capabilities of IoT applications and middleware platforms, thus the proposed PbD framework can also be used to design new IoT platforms.

## 2.2 Location Anonymization Approach for LBS

Location anonymization approach is one of most important techniques to protect location privacy, which attempts to make user's location indistinguishable from a certain number of other users. Commonly used techniques include spatial-temporal cloaking and location obfuscation.  $k$ -anonymity is an important technique for location anonymization, which relies on a centralized location anonymizer to enlarge a user's queried location into a bigger Cloaking Region (CR) for covering many other users. A personalized  $k$ -anonymity model is proposed in [23]. The model enables a user to have different privacy requirements in different contexts, and different users can require different levels of privacy in the same context. In the proposed model in [23], the trusted anonymization server runs an efficient message perturbation engine, which performs location anonymization considering the trade-off between location privacy and quality of service (QoS). A cloaking algorithm based on  $k$ -anonymity and  $l$ -diversity has been proposed in [24]. When constructing a cloaking region, it ensures that a cloaking region has at least  $k$  vehicles ( $k$ -anonymity) and  $l$  road segments ( $l$ -diversity), which can effectively protect user's location privacy. The authors in [25] studied the problem that how to protect the location privacy under various privacy threats, and proposed a location privacy framework uses  $k$ -anonymization and pseudo-anonymization methods to provide efficient location privacy preservation. A weighted adjacency graph based  $k$ -anonymous cloaking technique is proposed in [26], which can support  $k$ -nearest neighbor queries without revealing private information of the query initiator. The algorithm in [26] not only can ensure user privacy protection, but also reduce bandwidth usages. The concept of mix zones is first proposed in [27]. A mix zone is referred to a spatial region in which none of users has registered any application callback. The

authors in [28] allowed users to exchange their pseudonyms when they meet in a mix zone, which ensures a user avoid using a long-term pseudonym. Thus, the relationship between user pseudonyms and locations can be broken though exchanging pseudonyms.

## 2.3 Policy or Cryptography Primitive based Approach

Policy and cryptography primitive based approaches [29-31] protect user privacy by using encryption techniques. The authors in [32] propose a privacy preserving framework (PLAM) for local-area mobile social networks. The PLAM framework not only employs a privacy-preserving request aggregation protocol with  $k$ -anonymity and  $l$ -diversity properties to keep user's preference privacy without adopting a trusted anonymizer server when querying location-based service, but also integrates unlinkable pseudo-ID technique to achieve users' identity privacy and location privacy. The PLAM framework can not only satisfy the desirable privacy requirements but also resist outside attacks on source authentication, data integrity and availability. For preserving user's privacy, the authors in [33] proposed a dynamic pseudo-ID scheme, where different pseudo-IDs are adopted in different queries in order to unlink the correlation between user's real identity and trajectory. In [34], the authors propose a fine-grained privacy preserving LBS framework (FINE) for mobile devices. The FINE framework not only employs a ciphertext-policy anonymous attribute based encryption technique to achieve fine-grained access control, location privacy, confidentiality of the LBS data and its access rule, and accurate LBS query result without involving any trusted third party, but also integrates the transformation key and proxy re-encryption to migrate most of computation intensive tasks from LBS provider and users to cloud server. In [35], the authors study the  $k$  nearest neighbor (kNN) queries where mobile users query the LBS provider about  $k$  nearest points of interests (POIs) on the basis of their current location, and then propose a solution built on the Paillier public-key cryptosystem for preserving the location privacy and data privacy in kNN queries of mobile users. The authors in [36] design a private block retrieval protocol, and propose a secure and efficient location based service system. In the proposed system, users can retrieve information of interest associated with the current location without leaking their location information to the service provider.

## 2.4 Dummy Location Selection for IoT

Dummy location approach focuses on selecting dummy locations for users in order to protect users' location privacy. In [20], the authors first study the behaviors of self-interested users in the LBS system from a game-theoretic perspective. The work then formulates two Bayesian game models in both static and timing-aware contexts, and analyzes the existence and properties of the Bayesian Nash Equilibrium for the two models. A Dummy-Location Selection (DLS) algorithm is proposed in [22] to achieve  $k$ -anonymity for users using LBS. The DLS algorithm selects dummy locations considering that

the side information may be exploited by adversaries, which is based on the entropy metric [37]. To make sure that the selected dummy locations are spreaded as far as possible, the authors in [22] also propose an enhanced-DLS algorithm, which can enlarge the cloaking region while keeping similar privacy level as the DLS algorithm. The authors in [38] propose two dummy generation methods: circle-based and grid-based, which take into account privacy area requirements. In [39], the authors proposed two dummy based solutions to achieve  $k$ -anonymity for privacy-area aware users in LBS with considering that side information may be exploited by adversaries.

However, most of these existing approaches have not considered the side information that may be exploited by attackers when selecting dummy locations in IoT. Even if some approaches have taken into account the side information, but the computational costs (i.e., time complexities) of them are very high. Therefore, how to efficiently select dummy locations in IoT still remains a challenge, and our proposal will be presented between Section 3 and 6.

### 3. PRELIMINARIES

In this section, we describe the main basic concepts and the system model.

#### 3.1 Side Information

As mentioned in previous section, the side information [21] may be query probability of users related to location and time, or information related to the semantics of the query such as the gender and social status of the user. In this paper, the side information is considered to be the query probability of users related to location, called query probability. A particular user's query probability at a certain location can be denoted by the ratio of the number of current location queries to the number of total queries of all locations, as shown in Equation (1).

$$q_i = \frac{\text{number of queries in location } i}{\text{number of queries in all locations}} \quad (1)$$

Generally, users can get two kinds of side information from a system: *partial information* and *global information*. Partial information denotes the information collected by other users, for example, a particular user may know the query probabilities related to some locations. Since the LBS server can receive the LBS queries of all users, the LBS server can obtain the global information (i.e., the query probabilities related to all locations). For a particular user, it's necessary to design an optimal strategy to select dummy locations for protecting his/her location privacy under the condition of knowing the global information. In this paper, the LBS server is responsible for disseminating and updating the global side information so that users can get this information from a well-known place (e.g., local database of LBS application).

#### 3.2 Entropy-based Privacy Metric

In this work, the degree of privacy is measured by the entropy. It can be seen as the uncertainty in identifying a user's real location out from the chosen dummy locations [37]. When calculating the entropy, each dummy location should have a probability, which can be the history query probability of users related to location. We use  $p_i$  to denote the historic query probability of users related to location  $i$ . According to the set of dummy locations and the historic query probabilities, we can define the entropy  $H$  of a user as in Equation (2).

$$H = -\sum_{i=1}^k q_i \log_2 q_i \quad (2)$$

where  $q_i = p_i / \sum_{i=1}^k p_i$ , is the normalized query probability of location  $i$ ; and the sum of all  $p_i$  is equal to 1.

Since the greater the entropy the higher the uncertainty in identifying the user's real location from the dummy locations set, our goal is to obtain enough entropy. In particular, when all of the  $k$  dummy locations have the same historical query probability, we can achieve the maximum entropy  $H_{max} = \log_2 k$ .

#### 3.3 System Model for IoT

We design our system model based on the system architecture in [19]. The system mainly consists of two parties: the *LBS server* and *LBS users* with mobile devices.

1) LBS server: The LBS server can be a service provider, which not only stores all kinds of service databases, but also can update the service data and provide users with various services. In our system, the LBS server is responsible to receive service queries from users, search for requested service data in the database, and reply with the search results back to the users. In addition, the LBS server is able to obtain the global information based on queries of all users at all locations, which can be the historical query probabilities of users related to all locations. Moreover, the LBS server is responsible for disseminating and updating the global side information so that users can get this information from a well-known place (e.g., local database of LBS application).

2) LBS users: The system typically consists of users who are equipped with mobile devices (e.g., smart phones or tablets), with built-in GPS modules that can be used to obtain user's location data. Due to the rapid development of mobile devices and social networks, a variety of LBS applications can be accessible for users. If users want to get services from LBS servers, they need to send queries to LBS server, which include their identity, location information, interests, and the query range (e.g., 1000m). In order to protect user's location privacy, user's location information not only includes user's real location, but also includes many other dummy locations.



## 4. ANALYSIS OF THE DLS ALGORITHM

### 4.1 Review the DLS Algorithm

The main purpose of Dummy-Location Selection (DLS) algorithm [22] is to generate a set of realistic dummy locations to protect user's location privacy. Given the degree of anonymity  $k$ , the DLS algorithm needs to select other  $k-1$  dummy locations based on the side information. The following shows the 5 steps how the DLS algorithm addresses this problem:

(i) In the first step, a particular user needs to determine the degree of anonymity  $k$ .

(ii) Then, the algorithm reads all of the obtained query probabilities and then sorts the query probabilities of all locations in ascending order.

(iii) In the sorted list, the algorithm needs to choose  $2k$  candidate locations, whose history query probabilities are similar to the user's real location. In the  $2k$  candidate locations, it randomly selects  $k-1$  locations. Then, it derives  $m$  sets, each set contains  $k$  locations. For each set, one location is user's real location and the other  $k-1$  locations are randomly chosen from the  $2k$  candidates. The entropy for the  $j^{\text{th}}$  ( $j \in [1, m]$ ) set can be calculated according to Equation (2) as shown in Section 3.

(iv) Finally, the algorithm has to determine an optimal location set with the biggest entropy to effectively achieve  $k$ -anonymity for the user.

### 4.2 Preparations for Performance Analysis

**Table 1:** Summary of key notations

Notation	Meaning
$N$	Number of all locations.
$k$	The privacy level requirement of user.
$P[N]$	The historical query probabilities in all locations.
$m$	Number of randomly selecting $k-1$ locations from $2k$ locations, i.e., $m = C_{2k}^{k-1}$ .
$P_i$	The historical query probability at location $i$ .
$L_{\text{real}}$	The real location of user.
$P_i[2k]$	The chosen $2k$ candidates at location $i$ , where $k$ candidates are left before $L_{\text{real}}$ and the other $k$ candidates are right after $L_{\text{real}}$ in the sorted list.
$C_i[k]$	The chosen optimal location set at location $i$ .
$k'$	The number of locations which have the same historical query probability as $L_{\text{real}}$ in $P_i$ .

Let the historical query probabilities of all locations  $P = [p_1, p_2, \dots, p_N]$ , the chosen  $2k$  candidate locations at location  $i$  as  $P_i = \{p_{i,1}, p_{i,2}, \dots, p_{i,2k}\}$  and the chosen  $2k$  candidate locations at location  $j$  as  $P_j = \{p_{j,1}, p_{j,2}, \dots, p_{j,2k}\}$ . Then, let  $P_{ii} = P_i \cup \{p_i\}$ , and  $P_{ij} = P_{ii} \cap P_{jj}$ . Let  $M$  denote the size of set  $P_{ij}$ . We define  $P_{ij}$  as follows.

$$P_{ij} = \begin{cases} \{p_{(1)}, p_{(2)}, \dots, p_{(M)}\}, M > 0 \\ \emptyset, M = 0 \end{cases} \quad (3)$$

**Theorem 1:** Under the condition of  $m = C_{2k}^{k-1}$ , for  $\forall i, j \in [1, N]$ ,  $C_i \neq C_j$  ( $i \neq j$ ), set  $P$  must satisfy the following conditions:

(i)  $\forall i \neq j, p_i \neq p_j$ , i.e., each location has a unique historical query probability.

(ii)  $0 \leq M \leq 2k, \forall i, j$  ( $i \neq j$ ),  $P_{ij} \cap C_i \neq C_i$  or  $P_{ij} \cap C_j \neq C_j$ ; that is to say when  $0 \leq M \leq 2k, \forall i, j$  ( $i \neq j$ ), the chosen optimal location set at location  $i$  or location  $j$  is not included in the intersection of the chosen  $2k$  candidate locations at location  $i$  and the chosen  $2k$  candidate locations at location  $j$ .

**Proof:**

#### Adequacy:

(1) We first prove that set  $P$  must satisfy condition (i).

We assume that set  $P$  does not satisfy condition (i), and then  $\exists i, j \in [1, N], p_i = p_j$  ( $i \neq j$ ). Thus,  $P_i$  and  $P_j$  will be the same according to the step (ii) in DLS algorithm.

When  $k' \geq k + 1$ , although  $C_i$  may not be the same as  $C_j$  according to the step (iii) and (iv) in DLS algorithm, it is possible that  $C_i = C_j$ . However, according to our assumption that  $C_i$  cannot be the same as  $C_j$ . Thus, set  $P$  must satisfy condition (i).

When  $k' \leq k$ ,  $C_i$  must be the same as  $C_j$  according to steps (iii) and (iv) in DLS algorithm. However, according to our assumption,  $C_i$  cannot be the same as  $C_j$ . Thus, set  $P$  must satisfy condition (i).

(2) We then prove that set  $P$  must satisfy condition (ii) after satisfying the condition (i).

We assume that set  $P$  satisfies condition (i), but does not satisfy condition (ii). Thus,  $\exists i, j \in [1, N], P_{ij} \cap C_i = C_i$  and  $P_{ij} \cap C_j = C_j$ . Since  $C_i$  and  $C_j$  both are the optimal location set in set  $P_{ij}$ , i.e.,  $C_i = C_j$ . However, according to our assumption, set  $C_i$  cannot be the same as set  $C_j$ . Thus, set  $P$  must satisfy condition (i) and condition (ii).

#### Necessity:

According to condition (i), we can get that for  $\forall i \neq j, P_i \neq P_j$ . Then, we discuss the condition (ii) as follows.

(1)  $0 \leq M \leq 2k, \forall i \neq j, P_{ij} \cap C_i \neq C_i$  and  $P_{ij} \cap C_j \neq C_j$ . For this situation, set  $C_i$  must include the location from set  $P_i - P_{ij}$ , which does not belong to set  $C_j$ . Moreover, set  $C_j$  must also include the location from  $P_j - P_{ij}$ , which does not belong to set  $C_i$ . Thus, for  $\forall i \neq j, C_i \neq C_j$ .

(2)  $0 \leq M \leq 2k, \forall i \neq j, P_{ij} \cap C_i \neq C_i$  and  $P_{ij} \cap C_j = C_j$ . For this situation, set  $C_i$  must include the location from set  $P_i - P_{ij}$ , which does not belong to set  $C_j$ . Therefore, for  $\forall i \neq j, C_i \neq C_j$ .

(3)  $0 \leq M \leq 2k, \forall i \neq j, P_{ij} \cap C_i = C_i$  and  $P_{ij} \cap C_j \neq C_j$ . For this situation, set  $C_j$  must include the location from set  $P_j - P_{ij}$ , which does not belong to set  $C_i$ . Thus, for  $\forall i \neq j, C_i \neq C_j$ .

Therefore, we can conclude that for  $\forall i \neq j, C_i \neq C_j$  when set  $P$  satisfies conditions (i) and (ii).

### 4.3 Performance Analysis for DLS Algorithm

Based on step (iii) in the DLS algorithm, we can see that the greater of value of  $m$  the higher the computational cost of the DLS algorithm is. We also can see that different values of

$m$  may result in different optimal location sets in DLS algorithm, and the DLS algorithm can obtain the optimal location set when  $m = C_{2k}^{k-1}$ . We analyze the performance of the DLS algorithm when  $m = C_{2k}^{k-1}$  as follows.

(1)  $\exists i, j \in [1, N], p_i = p_j (i \neq j)$  in set  $P$ . We assume that a particular user is at location  $i$ , and the number of locations whose query probabilities are the same as that of the user's real location in the chosen candidate locations is denoted by  $k'$ . Since  $p_i = p_j$ , set  $P_i$  the user selects at location  $i$  is the same as set  $P_j$  the user selects at location  $j$  in DLS algorithm. We then discuss the performance of the DLS algorithm in the following situations. When  $1 \leq k' \leq k-1$ , set  $C_i$  is the same as set  $C_j$  in DLS algorithm under the condition  $m = C_{2k}^{k-1}$ . In this situation, although the LBS server can infer the probability for a user to submit a LBS query, the server cannot know the user's real location. This is because there are other locations whose query probabilities are the same as that of the user's real location. Moreover, the larger  $k'$  is, the better the performance of the DLS algorithm is. When  $k' \geq k$ ,  $C_i$  may be different from  $C_j$ . The reason is that randomly selecting  $k-1$  locations from the  $k'$  locations whose query probabilities are the same as  $p_i$  may be the optimal location set. In this situation, since each location has the same query probability, the DLS algorithm achieves the best performance.

(2)  $\forall i, j \in [1, N], p_i \neq p_j (i \neq j)$  in set  $P$ . We assume that a particular user is at location  $i$ . Since  $p_i \neq p_j$ , set  $P_i$  the user selects at location  $i$  must be different from the set  $P_j$  user selects at location  $j$ . However, when  $M \geq k-1$ ,  $C_i$  may be the same as  $C_j$ , that is to say the chosen optimal location set at location  $i$  is likely to be the same as the chosen optimal location set at location  $j$ . In this situation, although the LBS server may try to infer which location is most likely to select this location set, the server may make a incorrect decision. The reason is that the optimal location sets chosen by the user in other locations are the same as that of the user's real location. Moreover, the larger the number of locations whose chosen optimal location sets are the same as the that of user's real location is, the better the performance of the DLS algorithm is. However, once there is no location whose chosen optimal location set is the same as other locations in set  $P$ , the DLS algorithm would have bad performance.

## 5. ADLS ALGORITHM DESIGN

In this section, we first introduce an attack model and related theories, then give detailed descriptions of ADLS algorithm and the performance evaluations.

### 5.1 Attack Model

In order to protect location privacy, the dummy location generation algorithm is used for generating some dummy locations. Thus, the users' location information not only includes users' real location, but also includes other chosen dummy locations [38]. The goal of the adversary is to obtain the user's real location from the user's location information. Since adversaries can compromise the LBS server and obtain

all the information that the LBS server knows and holds. Thus, in this work, we assume that the LBS server is the adversary. Note that, LBS server is able to obtain global side information and monitor the current queries being sent from users. Furthermore, the LBS server can obtain the historic data of a particular user as well as the current situation and information. Additionally, the mechanisms used for location privacy protection in the system are also known by the LBS server.

### 5.2 Related Theories

Let set  $P = [p_1, p_2, \dots, p_n]$ , where  $0 < p_i < 1 (1 \leq i \leq n)$ . We define function  $H(P, p_{n+1})$  in Equation (4).

$$H(P, p_{n+1}) = - \sum_{p_i \in P} \frac{p_i}{\sum_{p_i \in P} p_i + p_{n+1}} \ln \frac{p_i}{\sum_{p_i \in P} p_i + p_{n+1}} - \frac{p_{n+1}}{\sum_{p_i \in P} p_i + p_{n+1}} \ln \frac{p_{n+1}}{\sum_{p_i \in P} p_i + p_{n+1}} \quad (4)$$

$$D(P, p_{n+1}) = \frac{dH(P, p_{n+1})}{dp_{n+1}} = \frac{\sum_{p_i \in P} p_i \ln p_i - \sum_{p_i \in P} p_i \ln p_{n+1}}{(\sum_{p_i \in P} p_i + p_{n+1})^2} \quad (5)$$

In Equation (4), function  $H(P, p_{n+1})$  varies with  $p_{n+1}$ , where  $0 < p_{n+1} < 1$ . In order to get the maximum value of  $H(P, p_{n+1})$ , we first calculate the derivative of function  $H(P, p_{n+1})$ , denoted by function  $D(P, p_{n+1})$  as shown in Equation (5). Then, let function  $D(P, p_{n+1})$  be zero to get the value of  $p_{n+1}$  as shown in Equation (6). Finally, we can get the extreme points of function  $H(P, p_{n+1})$ . From Equation (6), we can know that function  $H(P, p_{n+1})$  has a unique extreme point.

$$\frac{\sum_{p_i \in P} p_i \ln p_i - \sum_{p_i \in P} p_i \ln p_{n+1}}{(\sum_{p_i \in P} p_i + p_{n+1})^2} = 0 \Rightarrow \sum_{p_i \in P} p_i \ln p_i - \sum_{p_i \in P} p_i \ln p_{n+1} = 0 \Rightarrow p_{n+1} = \exp\left(\frac{\sum_{p_i \in P} p_i \ln p_i}{\sum_{p_i \in P} p_i}\right) \quad (6)$$

$$\text{Let } \bar{p}_{n+1} = \exp\left(\frac{\sum_{i=1}^n p_i \ln p_i}{\sum_{i=1}^n p_i}\right).$$

When  $p_{n+1} < \bar{p}_{n+1}$ , the value of function  $D(P, p_{n+1})$  is greater than zero, and the value of function  $H(P, p_{n+1})$  increases with the growth of  $p_{n+1}$ . When  $p_{n+1} > \bar{p}_{n+1}$  the value of function  $D(P, p_{n+1})$  is less than zero, the value of function  $H(P, p_{n+1})$  decreases with the growth of  $p_{n+1}$ . Thus, we have that the maximum point of function  $H(P, p_{n+1})$  is  $p_{n+1} = \bar{p}_{n+1}$ . We can obtain the range of  $\bar{p}_{n+1}$  by Equation (7). From Equation (7), we can see that the value of  $p_{n+1}$  is not greater than the

maximum of set  $P$ , and also not less than the minimum of set  $P$ . In our ADLS algorithm, we can use this property to select dummy locations.

$$\begin{aligned}
& \min(P) \leq p_i \leq \max(P) \\
& \Rightarrow \ln(\min(P)) \leq \ln p_i \leq \ln(\max(P)) \\
& \Rightarrow \ln(\min(P)) \sum_{p_i \in P} p_i \leq \sum_{p_i \in P} p_i \ln p_i \leq \ln(\max(P)) \sum_{p_i \in P} p_i \quad (7) \\
& \Rightarrow \min(P) \leq p_{n+1} = \exp\left(\frac{\sum_{p_i \in P} p_i \ln p_i}{\sum_{p_i \in P} p_i}\right) \leq \max(P)
\end{aligned}$$

### 5.3 The ADLS Algorithm

The main goal of the ADLS algorithm is to identify the user's real location out from the dummy locations obtained by the DLS algorithm. When obtaining a user's LBS query, an adversary can adopt two methods to infer the user's real location based on user's location information. One method is to randomly choose one location from user's location information as the user's real location. By this method, the probability of successfully identifying the user's real location is  $1/k$ , and the probability remains stable. The other method is to analyze the dummy location generation algorithm, and then design an attack algorithm. By this method, the adversary can enhance the probability of successfully identifying the user's real location by designing a good attack algorithm. In this paper, we adopt the latter method to infer user's real location. Based on the analysis of the DLS algorithm in section 4, we know that once the history query probabilities of two locations are different in DLS algorithm, their chosen optimal dummy location sets must be different. In this paper, we use this property to infer the user's real location out from the user's location information.

The ADLS algorithm first gets the anonymity degree  $k$  according to the user's location information. Then, for the  $i^{\text{th}}$  ( $1 \leq i \leq k$ ) location in user's location information, the ADLS algorithm selects other  $k-1$  dummy locations based on entropy in a greedy manner, and then obtains the dummy location set  $C_i$ . After obtaining the  $k$  dummy location sets, the ADLS algorithm sorts the probabilities of set  $C_i$  ( $1 \leq i \leq k$ ) and the user's dummy location set in ascending order. Then, for each dummy locations set  $C_i$  ( $1 \leq i \leq k$ ), the ADLS algorithm calculates the variance between the set  $C_i$  and the user's dummy location set, and determines the user's real location based on the variance. For example, if the variance between the set  $C_i$  and the user's dummy location is the smallest, the ADLS algorithm infers that the user's real location is location  $i$ . The following shows how the ADLS algorithm works.

(i) In the first step, the LBS server needs to get the anonymity degree of a user based on the user's location information. Let  $k$  denotes a user's anonymity degree, set  $R$  denotes a user's location information.

(ii) LBS server reads all the query probabilities and then sorts query probabilities of all locations in ascending order.

(iii) For each location in set  $R$ , the LBS server needs to selects  $2k-2$  candidate locations (denoted as set  $D_j$ ), in which  $k-1$  locations are left before the user's real location and the other  $k-1$  locations are right after the user's real location in the sorted list. Then, the LBS server puts the user's real location in  $C_j$  ( $j \in [1, k]$ ).

(iv) Find the maximum and minimum from set  $C_j$ . Let  $p_{\max}$  denote the maximum and  $p_{\min}$  denote the minimum. Then, it finds two locations in set  $D_j$ , which is the maximum of the probability set being less than  $p_{\min}$ , denoted by  $p_{\min-\max}$ , and the other is the minimum of the probability set being greater than  $p_{\max}$ , denoted by  $p_{\max-\min}$ . Finally, it compares the entropy  $H(C_j, p_{\max-\min})$  and  $H(C_j, p_{\min-\max})$ , and puts the location in set  $C_j$ , which achieves a larger entropy.

(v) Repeat step (iv) until the size of set  $C_j$  is  $k$ .

(vi) Finally, LBS server needs to determine which one is the user's real location. Specifically, for a particular chosen set  $C_j$ , it computes the variance according to Formula (8).

$$S_j = \sum_{i=1}^k (r_i - c_i)^2 \quad (8)$$

where  $r_i \in R$ ,  $c_i \in C_j$ . The ADLS algorithm then uses the locations with the least variance as the user's real location:

$$S = \arg \min S_j \quad (9)$$

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#### Algorithm 1: Attack algorithm for DLS (ADLS)

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**Input:** Historical query probabilities of all locations denoted as  $P$ ; a user's location information  $R$ .

**Output:** The optimal location.

- 1: Sort the elements in  $P$  and  $R$  in ascending order;
- 2:  $k \leftarrow$  user's anonymity degree
- 3: **for** ( $i=1; i \leq k; i++$ ) **do**
- 4:   Set  $C_i \leftarrow$  read one location  $L$  from set  $R$  which isn't read before;
- 5:   Choose  $k-1$  locations left before and  $k-1$  locations right after location  $L$  in the sorted list as candidate location set  $D_i$ ;
- 6:   **for** ( $j=1; j \leq k; j++$ ) **do**
- 7:      $p_{\max} \leftarrow \max(C_i)$ ;
- 8:      $p_{\min} \leftarrow \min(C_i)$ ;
- 9:     Find one location from set  $D_i$ , which is the maximum of the probability set being less than  $p_{\min}$  in set  $D_i$ , denoted as  $p_{\min-\max}$ ;
- 10:     Find one location from set  $D_i$ , which is the minimum of the probability set being greater than  $p_{\max}$  in set  $D_i$ , denoted as  $p_{\max-\min}$ ;
- 11:     **if**  $H(C_i, p_{\max-\min}) > H(C_i, p_{\min-\max})$  **then**
- 12:        $C_i \leftarrow C_i \cup \{p_{\max-\min}\}$ ,  $D_i \leftarrow D_i \setminus \{p_{\max-\min}\}$ ;
- 13:     **else**
- 14:        $C_i \leftarrow C_i \cup \{p_{\min-\max}\}$ ,  $D_i \leftarrow D_i \setminus \{p_{\min-\max}\}$ ;
- 15:     **end**



16: end for  
17: Sort the elements in  $C_i$  in ascending order;  
18:  $S_i \leftarrow \sum_{i=1}^k (r_i - c_i)^2$   
19: end for  
20: return  $\arg \min S_i$

#### 5.4 Performance Evaluation

In this subsection, we evaluate the effectiveness of our proposed ADLS algorithm through simulation experiments.

##### 5.4.1 Simulation Environment

In this set of simulations, the service area of LBS provider is divided into  $n \times n$  cells with equal size. We assume that each cell has already had a historical query probability based on the users' previous queries. For measuring the *probability of query recognition*, which denotes the probability for the proposed ADLS algorithm to successfully identify a user's real location from the chosen dummy locations, we use the DLS algorithm to generate dummy locations and submit 1000 queries in the simulations.

In our simulations,  $k$  is related to  $k$ -anonymity and denotes the anonymity degree. Given the value of  $k$ ,  $m$  denotes the number of cases that randomly choose  $k-1$  cells from  $2k$  cells, whose maximum value is  $C_{2k}^{k-1}$ . For evaluating the ADLS algorithm, the following four scenarios are considered in our simulations:

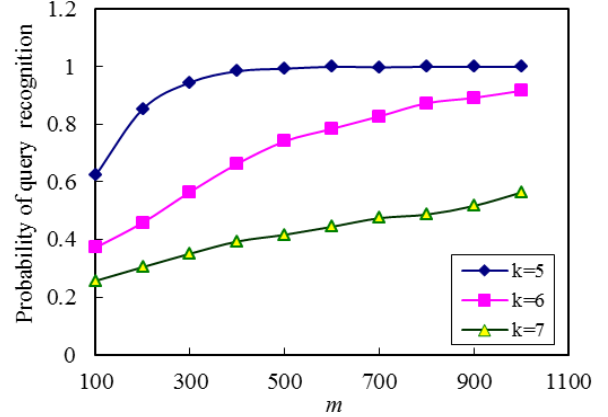
- *Scenario-1*: The value of  $m$  varies from 100 to 1000.
- *Scenario-1.1*: The value of  $k$  varies from 5 to 7.
- *Scenario-1.2*: The value of  $k$  varies from 10 to 14.
- *Scenario-2*: The value of  $k$  varies from 5 to 15, and the values of  $m$  are set to be  $1 \times 10^4$ ,  $5 \times 10^4$  and  $1 \times 10^5$ , respectively.

##### 5.4.2 Numeric Results

For evaluating the effectiveness of the proposed ADLS algorithm, we have conducted extensive simulations. We have evaluated the performance of the ADLS algorithm in terms of probability of query recognition under different scenarios with different values of  $k$  and  $m$ . Based on the analysis of the DLS Algorithm in Section 4, we can see that if a user's chosen optimal location set at location  $i$  is different from that of location  $j$  ( $i$  and  $j$  denote two different locations), the *ADLS Algorithm* with high probability to infer the user's real location from the dummy locations generated by DLS Algorithm.

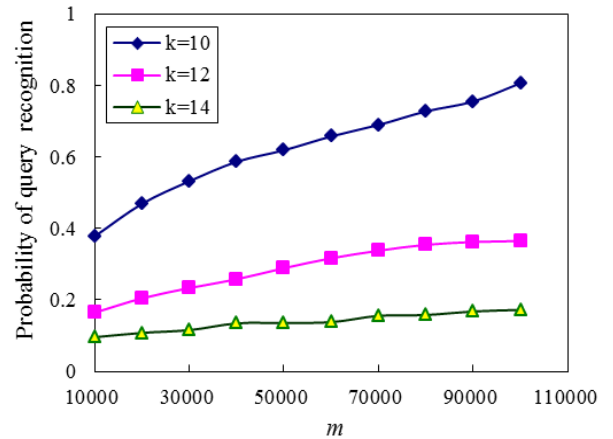
**Simulation Results Under Scenario-1.1:** We explore the relationship between  $m$  and the probability of query recognition. From Figure 1, we can see that the probability of query recognition generally increase with the growth of  $m$ . The reason is that larger  $m$  leads to the chosen dummy location in DLS algorithm to be closer to the optimal dummy location set, which enables the ADLS algorithm to identify the user's real location with high probability. Figure 1 also shows that greater  $k$  leads to lower probability of query

recognition while lower  $k$  results in higher probability of query recognition and this can be explained as follows. First, the maximum of  $m$  is  $C_{2k}^{k-1}$ , and  $C_{2k}^{k-1}$  exponentially increases with the growth of  $k$ . Second, for a given value of  $m$ , smaller anonymity degree  $k$  results in that the value of  $m$  is more close to the maximum one. Therefore, the user's chosen dummy locations are more likely to be close to the optimal dummy locations.



**Fig.1:** The probability of query recognition achieved with different anonymity degrees  $k$  under Scenario-1.1.

**Simulation Results Under Scenario-1.2:** In this set of simulations, we explore the relationship between  $m$  and the probability of query recognition when  $m$  and  $k$  become greater. Comparing with the results of Scenario-1.1, we observe that although the value of  $m$  and the value of  $k$  become greater, the probability of query recognition does not be improved. The reason is that when the value of  $k$  becomes greater, the higher probability of query recognition can be obtained only with greater value of  $m$ . Moreover, a small difference in the anonymity degree  $k$  will lead to a great difference in the value of  $m$  when achieving the same probability of query recognition in the ADLS algorithm.



**Fig.2:** The probability of query recognition achieved in different anonymity degree  $k$  under Scenario-1.2.

**Simulation Results Under Scenario-2:** Figure 3 shows the relationship between  $k$  and the probability of query recognition. Generally, for a given value of  $m$ , the probability

of query recognition will be influenced by the value of  $k$ . The results show that the greater the value of  $k$  is, the lower the probability of query recognition is. Furthermore, greater  $m$  leads to higher probability of query recognition while lower  $k$  results in lower probability of query recognition when  $k \geq 8$ . Moreover, different values of  $m$  have almost the same probability of query recognition when  $k \leq 7$ . The reason is that the smaller  $k$  makes the value of  $m$  to be close to the maximum value. Therefore, the user can select the optimal location set with higher probability.

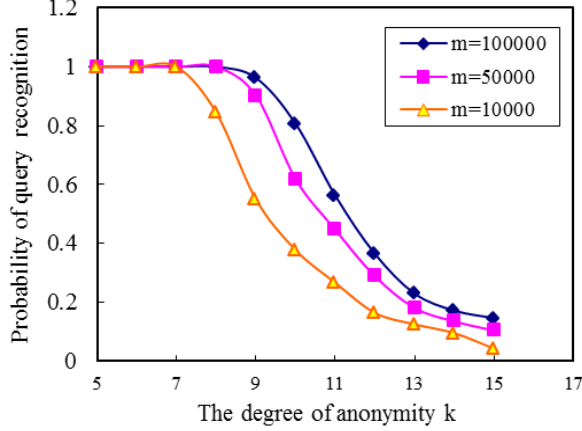


Fig.3: The probabilities of query recognition under Scenario-2.

## 6. DLP ALGORITHM DESIGN AND ANALYSIS

In this section, we give the detailed descriptions for the DLP algorithm, and present the performance evaluations.

### 6.1 DLP Algorithm Description

The basic idea of Dummy Location Privacy-preserving (DLP) algorithm is to select the optimal dummy locations considering that the adversary may exploit some side information, and make different choice for different privacy requirements of different users. We adopt a greedy approach to search a large database to find an optimal set of dummy locations. For achieving  $k$ -anonymity, we successively select  $k-1$  other locations from all locations in the location map, which must make sure that the current entropy is the biggest. For example, if the DLP algorithm has already chosen  $i$  locations (where  $i < k$ ), when choosing the  $(i+1)^{th}$  location, it must ensure that  $H_{i+1}$  is the largest for all residual locations.  $H_{i+1}$  is defined in Equation (10).

$$H_{i+1} = -\sum_{j=1}^{i+1} \frac{p_j}{\sum_{l=1}^{i+1} p_l} \log_2 \frac{p_j}{\sum_{l=1}^{i+1} p_l}, \quad (10)$$

where  $p_j$  denotes the users' historical query probability at location  $j$ . The following shows how the proposed DLP algorithm works.

(i) First, a user needs to set a proper anonymity degree  $k$ ,

which is closely related to the user's requirement on location privacy. Although a bigger  $k$  leads to higher anonymity degree, it also causes a higher overhead due to the cost for selecting dummy locations.

(ii) At the beginning, the DLP algorithm needs to read all the obtained query probabilities from the LBS server and then sort the query probabilities in ascending order. Let  $p$  denote the query probability of the user's real location. For the sorted list, the DLP algorithm calculates the number of locations which have the same query probability as  $p$ , which is denoted by  $\bar{k}$ . If  $\bar{k}$  is large enough, it puts half of them before and the other half of them after the real location.

(iii) If  $\bar{k} \geq k$ , DLP algorithm selects  $k-1$  locations which have the same query probability as  $p$  from the sorted list. Then, it outputs the chosen  $k-1$  dummy location and the user's real location.

(iv) If  $k/4 \leq \bar{k} < k$ , the algorithm selects  $\bar{k}-1$  locations which have the same query probability as  $p$  from the sorted list. We use set  $C$  to denote the  $\bar{k}-1$  dummy locations and the user real location. In the sorted list, the algorithm selects  $k-\bar{k}$  locations left before and other  $k-\bar{k}$  locations right after the real location as  $2(k-\bar{k})$  candidate locations, whose query probabilities are different from  $p$ . Let set  $S$  denotes the  $2(k-\bar{k})$  candidates. The reason for choosing  $2(k-\bar{k})$  candidates for dummy locations is to make sure to get large enough entropy. Otherwise, it goes to Step (vii).

(v) To achieve  $k$ -anonymity, it needs to successively select residual  $k-\bar{k}$  locations from set  $S$ . For the  $i^{th}$  ( $\bar{k} < i \leq k$ ) dummy location, it must ensure that the  $H_i$  is maximum for all residual locations in set  $S$ .

(vi) When the size of  $C$  is  $k$ , DLP outputs the set  $C$ .

(vii) If  $\bar{k} < k/4$ , the DLP chooses  $2k-\varepsilon$  locations left before and other  $2k-\omega$  locations right after the real location as  $4k-\omega-\varepsilon$  candidates from the sorted list. We use set  $\bar{S}$  to denote the  $4k-\omega-\varepsilon$  candidates. Both  $\omega$  and  $\varepsilon$  are set by users based on their privacy requirements. Generally,  $\omega$  is smaller than  $\varepsilon$ . Let set  $\bar{C}$  denote a user's real location. It randomly selects one location as a dummy location from set  $\bar{S}$ , and put this location into set  $\bar{C}$ .

(viii) For achieving  $k$ -anonymity, the successively selects residual  $k-2$  locations from set  $\bar{S}$ . For the  $i^{th}$  ( $2 < i \leq k$ ) dummy location, it must ensure that  $H_i$  is the largest for all residual locations in set  $\bar{S}$ .

(ix) When the size of  $\bar{C}$  is  $k$ , DLP outputs the set  $\bar{C}$ .

---

#### Algorithm 2: Dummy Location Privacy-preserving (DLP)

**Input:** The set of historical query probabilities  $P$ ; users' real location.

**Output:** The optimal set of dummy locations,  $C$ .

- 1: Sort  $P$  in ascending order;
- 2:  $H \leftarrow$  select the locations which have the same query probability as users' real location from sorted  $P$ ;
- 3: **if** ( $size(H) \geq k$ ) **then**

```

4:    $C \leftarrow$  randomly select  $k$  locations including the user
      real location from  $H$ ;
5: else if  $(k/4 < \text{size}(H) < k)$  then
6:    $\bar{k} \leftarrow \text{size}(H)$ ,  $C \leftarrow H$ ;
7:    $S \leftarrow$  choose  $2(k-\bar{k})$  candidate locations whose query
      probabilities are similar to the user's real location;
8:   for  $(j = 1; j \leq k-\bar{k}; j++)$  do
9:     Choose one location  $l$  from set  $S$ , such that  $H(C, q)$ 
      is the maximum in set  $S$ ;
10:     $C \leftarrow C \cup \{l\}$ ,  $S \leftarrow S \setminus \{l\}$ ;
11:  end for
12: else
13:   $S \leftarrow$  choose  $4k-\omega-\varepsilon$  candidate locations whose query
      probabilities are similar to the user's real location;
14:  Randomly choose location  $i$  from  $S$ ;
15:   $C \leftarrow H \cup \{i\}$ ;
16:  for  $(j = 1; j \leq k-2; j++)$  do
17:    Choose one location  $h$  from  $S$ , which makes
      sure that  $H(C, q)$  is the maximum in set  $S$ ;
18:     $C \leftarrow C \cup \{h\}$ ,  $S \leftarrow S \setminus \{h\}$ ;
19:  end for
20: end if
21: return the optimal set of dummy locations,  $C$ .

```

## 6.2 Security Analysis

This subsection shows that how to resist the *colluding attacks* and *inference attacks* to protect user's location privacy through the proposed DLP algorithm.

1) *Resistance to the Colluding Attack*: To obtain user's location privacy, passive attackers may collude with other users or with the LBS provider for various purposes.

**Definition 1**: A scheme can resist the colluding attack if the probability of successfully identifying a user's real location from the user's location information does not increase with the growth of the size of the colluding group.

**Theorem 1**: The DLP algorithm can resist the colluding attack.

*Proof*: A colluding attack happens among a set of users who want to identify a user's real location out from the submitted  $k$  locations. In our scheme, each user protects her/his location privacy by selecting other dummy locations. When an attacker first compromises a user  $U_A$ , he/she will obtain the user's location information including  $k$  locations. Since the  $k$  locations have similar historical query probabilities, the attacker has no clue about the user's real location and only randomly guesses the user's real location out from the intercepted  $k$  locations. Thus, the probability of successfully identifying the user's real location is  $1/k$ . Then, the attacker intercepts the LBS query of user  $U_B$ , and obtains the user's location information. However, the probability of successfully identifying a user's real location remains stable in our scheme. The reason is that there are no correlations between the selected dummy locations of users  $U_A$  and  $U_B$ . Therefore, the attacker can only identify each user's real

location randomly from the intercepted  $k$  dummy locations. Similarly, when a colluding group has more members involve, the attacker can only randomly guess each user's real location from the intercepted  $k$  dummy locations. This implies that the probability of successfully identifying the user's real location out from the chosen dummy locations remains stable (i.e.,  $1/k$ ) in our scheme.

In an extreme case that the passive adversary compromise the LBS server and get all information the LBS server has, he/she can turn to be an *active* adversary. For an active adversary, he/she can perform the inference attack.

2) *Resistance to the Inference Attack*: In this part of analysis, we assume that the LBS provider is an active attacker. The LBS provider knows a user's historical query probabilities of all locations, the historical queries and the current queries of users.

**Definition 2**: A scheme can resist the inference attack if attackers cannot successfully identify the user's real location from user's location information.

**Theorem 2**: DLP scheme can resist the inference attack.

*Proof*: In the DLP scheme, since the chosen  $k$  locations have similar historical query probabilities, although the LBS provider knows the historical query probabilities of all locations, he/she cannot determine which one is the user's real location in the  $k$  locations. Even then he/she tries to reverse the algorithm, but he/she will also be failed. The reasons are explained in the follows. Let us recall the step (3) to step (11) of the DLP scheme mentioned in Section 6.1. In these steps, since the DLP scheme can guarantee that there are enough locations whose historical query probabilities are as same as that of the user's real location in the chosen dummy locations, thus the LBS server still cannot obtain the user's real location by reversing the algorithm. Furthermore, let us recall the step (13) to step (18) of the DLP scheme. In these steps, since step (13) and step (14) of DLP can ensure the uncertainty of the selection, the LBS server also cannot obtain the real location by running our algorithm several times.

## 6.3 Performance Evaluation

For evaluating the performance of DLP algorithm, we have conducted extensive simulations in this subsection.

### 6.3.1 Simulation Environment

Similar to Section 5.4, we divide the location map into  $n \times n$  cells with equal size. Each cell has a query probability based on the query history. We conduct simulations on the following three scenarios to evaluate the performance of the DLP algorithm.

- **Scenario A**: Let user be located in a cell such that there are many (more than  $k$ ) cells that have the same historical query probability as the user's current location. In this scenario, the chosen dummy locations have the same query probability as that of the user's real location.
- **Scenario B**: Let user be located in a cell such that the number of cells that have the same historical query

probability as that of the user's current location is slightly less than  $k$  but greater than one quarter of  $k$ . In this scenario, it can guarantee that there are enough locations have the same query probability as that of the user's real location in the chosen dummy locations.

- **Scenario C:** Let user be located in a cell such that there are a few (i.e., less than one quarter of  $k$ ) cells have same historical query probability as that of the user's current location. In this scenario, there are few locations that have the same query probability as that of the user's real location in the chosen dummy locations.

### 6.3.2 Simulation Results

For evaluating the effectiveness of our proposed DLP algorithm, we have conducted extensive simulations. We have compared the performance of two algorithms in terms of the running time and the privacy level under various anonymity degree requirements of users. We also compare the probability of query recognition under Scenario C.

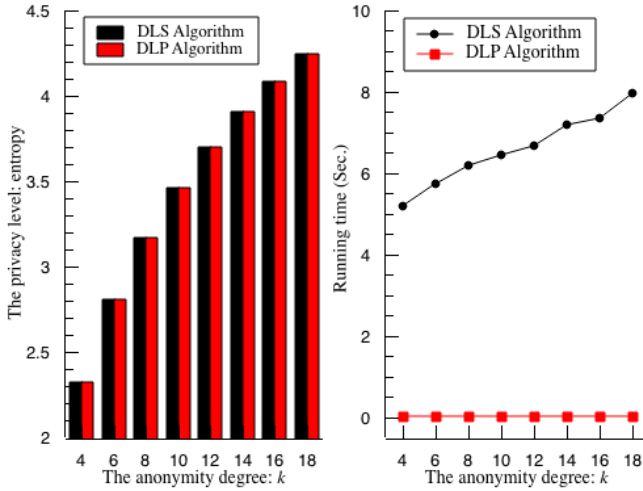


Fig.4: Entropy and running times under Scenario A

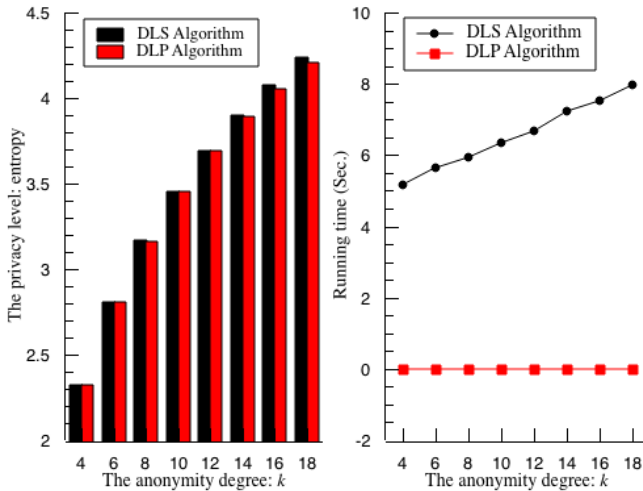


Fig.5: Entropy and running times under Scenario B

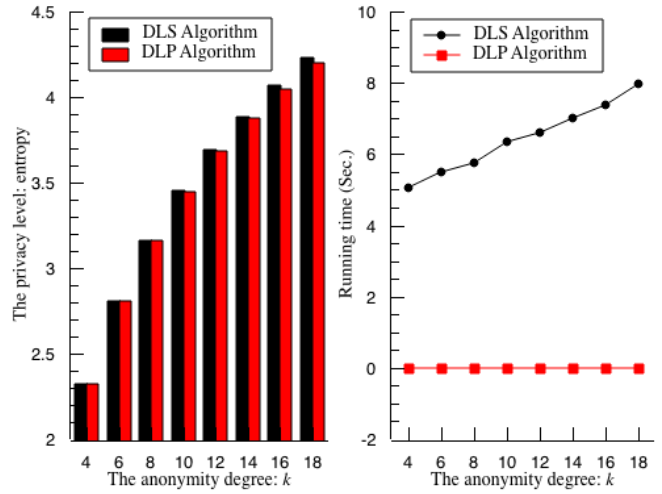


Fig.6: Entropy and running times under Scenario C

Figure 4, Figure 5 and Figure 6 illustrate the results for DLS algorithm and DLP algorithm, respectively. The results show the running time and the privacy level in terms of entropy under different scenarios. In Figure 4, the DLP algorithm and the DLS algorithm have the same entropy, but there are large differences in the running times. Moreover, the running time of DLS algorithm rapidly increases with the growth of the value of  $k$  (i.e., anonymity degree), but the running time of DLP algorithm varies little. The reason is that the DLS algorithm adopts enumeration method to select  $k$  dummy locations which make the entropy is largest while the DLP algorithm adopts greedy method to successively select  $k$  dummy locations. The computational complexity of the DLS algorithm increases with the growth of the value of  $k$ , but the computational complexity of the DLP algorithm almost remains stable. From Figure 5 and Figure 6, we can see that Scenario B and Scenario C have the similar trend on results as Scenario A. We also note that the largest entropy appears in Scenario A, whereas the smallest entropy appears in Scenario C for both the DLS and DLP algorithms. This is because that there are more than  $k$  locations whose historical query probabilities are the same as that of the user's real location in Scenario A, but there are only enough or few locations whose historical query probabilities are the same as that of the user's real location in Scenario B or C. Moreover, we can obtain the maximum entropy  $H_{max} = \log_2 k$  under Scenario A. Thus, the DLS and DLP algorithms can achieve larger entropy in Scenario A than that in Scenario B or C.

Figure 7 illustrates the probability of query recognition in the different schemes. The simulation results show that the DLP algorithm has lower probability of query recognition than the DLS algorithm under the same attack. Moreover, the probability of query recognition does not vary much with the anonymity degree  $k$  in the DLP algorithm compared with the DLS algorithm. Furthermore, although the probability of query recognition of the DLS algorithm decreased with the growth of the value of  $k$ , the probability of query recognition

is still higher than that of the DLP algorithm. In particular, when the number of cases for randomly selecting  $k-1$  cells from  $2k$  cells achieves the maximum  $C_{2k}^{k-1}$ , the probability of query recognition can be near 100% for the DLS algorithm. Therefore, the DLP algorithm has a better performance on probability of query recognition than DLS algorithm.

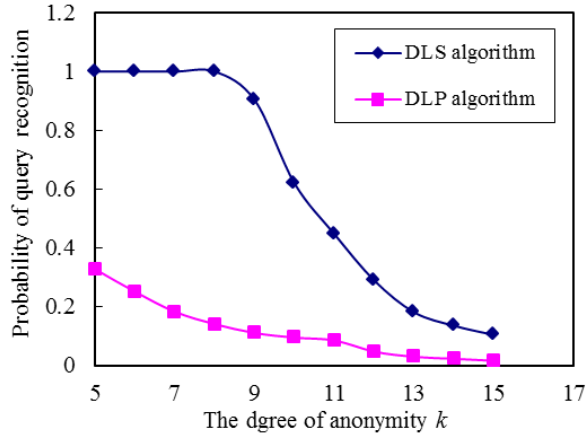


Fig.7: The probability of query recognition for Scenario C

## 7. DISCUSSION

Two topics, our contributions in the data-driven IoT service and the extension of this work, are presented for discussion.

### 7.1 Our contributions in data-driven IoT services

The data-driven IoT services take consideration for big data and IoT fusion which have become increasing important for security. Our contributions are summed up as follows. The DLP algorithm can satisfy velocity since the rate of data processing is fast and efficient, with a better performance than the competing DLS algorithm as demonstrated in Section 6.3. The DLP algorithm has been tested with three different user scenarios and results are consistent and accurate. Experiments with ADLS also support the consistency and accuracy of probability of query recognition. Thus, our work also satisfies veracity for data-driven IoT services. Finally, the cases presented in our paper illustrate that the DLP can be useful to protect the users' privacy and validate results with the users' real locations. Hence, validity for data-driven IoT services has been demonstrated in our theoretical development supported by simulation results.

### 7.2 Extension of Our Work

Multi-layered security proposed by Chang et al. [40] has demonstrated that penetration testing and ethical hacking of injecting 10,000 known viruses and Trojans in 2013 can be blocked and isolated, with 99.9% success rate. Multi-layered security can be blended with ADLS as an emerging IoT service to ensure that hacking by malicious files injections can be minimized. Experiments demonstrated by Chang and Ramachandran [41] have demonstrated that when 10 petabytes of data has been undergone for penetration ethical

tests, multi-layered security can block and kill 99.9% of known 2013 vulnerability. In addition, locations can be pointed back to the Data Center hosting secure mobile services, so that anyone who plan to track users, the only locations shown are the central server for mobile services without revealing the exact users' locations.

## 8. CONCLUSION

In this paper, we first theoretically analyze the performance of the Dummy-Location selection (DLS) algorithm, which is an efficient approach to protect users' location privacy in LBS for IoT. Then, we design an Attack algorithm for DLS algorithm (ADLS), whose goal is to identify the user's real location from chosen dummy locations generated by DLS algorithm. For efficiently preserving users' location privacy, we also propose a new Dummy Location Privacy-preserving (DLP) algorithm, which takes into account the equilibrium between the computational cost (i.e., time complexity) and the privacy requirements of users. Based on the obtained side information and the entropy metric, DLP algorithm greedily selects dummy locations to achieve the optimal privacy level of  $k$ -anonymity. We also analyze the security performance of the proposed DLP algorithm against potential attacks in the data-driven IoT service. Finally, we evaluate the performance of our DLP algorithm and ADLS algorithm by conducting extensive simulation experiments under various scenarios. Our simulation results show that our ADLS algorithm has high probability of identifying the user real location from the dummy locations generated by DLS algorithm. Moreover, comparing with the DLS algorithm, our DLP algorithm has lower probability of revealing the user real location under the same attack, and can reduce the computational cost (i.e., time complexity) when providing same privacy level as the DLS algorithm. We explain our contributions for the data-driven IoT service and justify that our work can make greater impacts while blending with multi-layered security to prevent attacks and preserve location privacy.

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